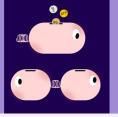
Economic Principles in Cell Biology

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Principles of cell growth

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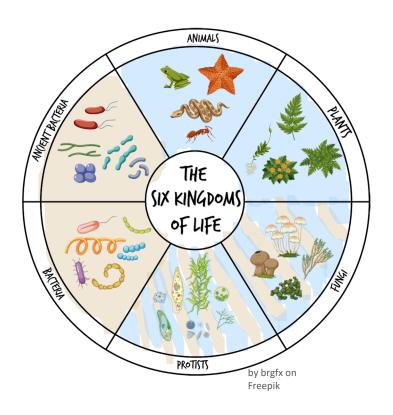
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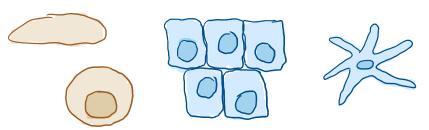




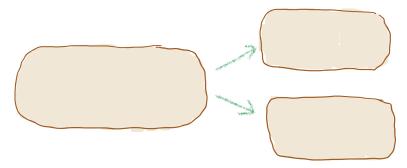
Self-replication is a hallmark of life



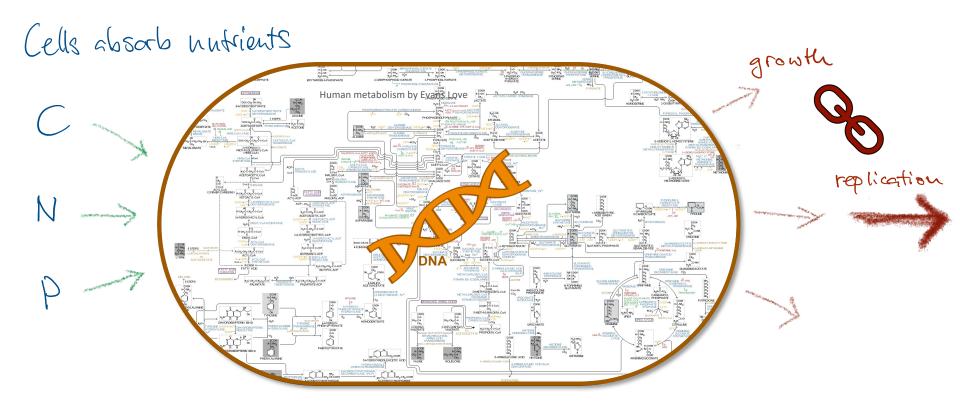
Cells are building blocks of life



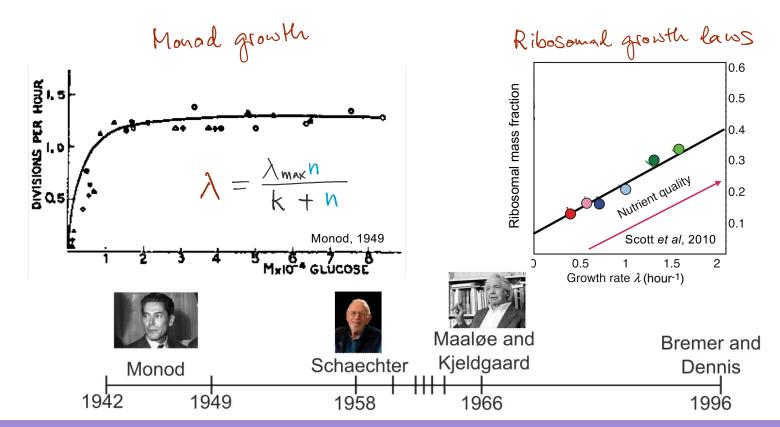
Cellular self-replication underpins reproduction of life



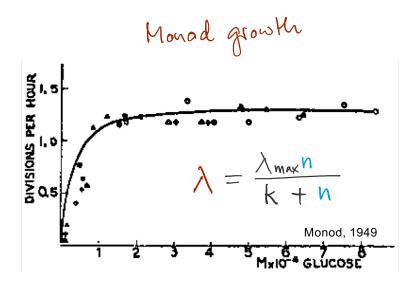
Self-replication is inherently coupled to growth



Growth laws govern the relation of growth with environmental & cellular features

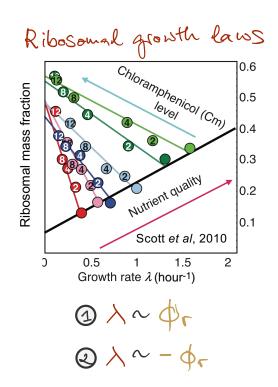


Growth laws govern the relation of growth with environmental & cellular features



Other growth laws:

- cell size
- cell surface
- nutrient influx...



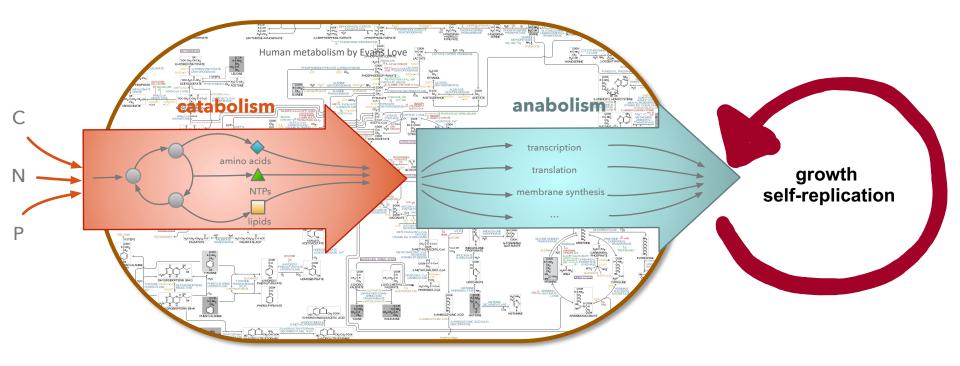
What model should we use?



Complex enough to explain

- 1. There is no one model.
- 2. What's the purpose of the model?

Many cell models share a common structure



Let's start with a simple growth model

growth rate

Two reactions:

$$\Lambda \stackrel{\vee_2}{\longrightarrow}$$



Assumptions:

Proteome dominates biomass



Cell has constant density

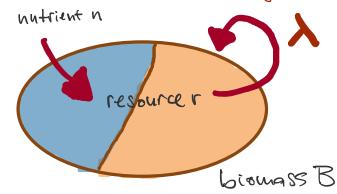
$$\mathcal{B} \sim V \implies \frac{\gamma}{\mathcal{B}} \sim \text{concentration of cell component y}$$

Reaction rates are proportional to protein concentrations

$$V_1 = \frac{P \mapsto r}{B} \cdot \beta_{n \to r}$$
 $V_2 = \frac{Pr \to B}{R} \cdot \beta_{r \to B}$

Steady-state assumption:

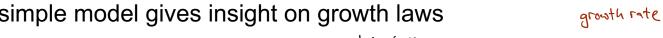
$$\dot{r} = \frac{dr}{dt} = V_1 - V_2 = 0 \iff V_1 = V_2$$

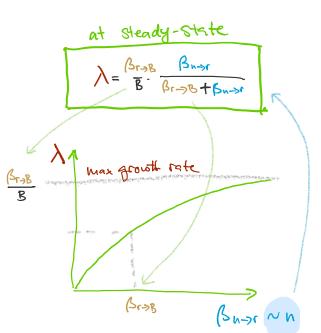


What determines the growth rate?

(1) - (1):
$$\frac{(B-Pr > B)}{B}$$
 $\beta_{N > r} = \frac{Pr > B}{B}$ $\beta_{r > r}$
 $\Rightarrow Pr > B = B \cdot \frac{B_{N > r}}{B_{r > r}}$ $\beta_{r > r}$
 $\Rightarrow \beta_{r > r} = \beta_{r > r}$ $\beta_{r > r}$
 $\Rightarrow \lambda = \frac{V_2}{B} = \frac{1}{B}$ $\beta_{r > r}$

The simple model gives insight on growth laws

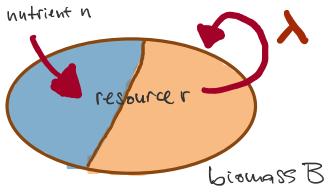




but also
$$\lambda = \frac{1}{B} \frac{Pr \rightarrow B}{B} \beta_{r \rightarrow R}$$

$$\Rightarrow \lambda \sim \frac{Pr \rightarrow B}{B}$$

Growth-ribosome relation



What determines the growth rate?

Further assume nutrient limiting

$$\Rightarrow \lambda \sim \frac{\lambda_{\text{max}} n}{k + n}$$
 Monod-growth

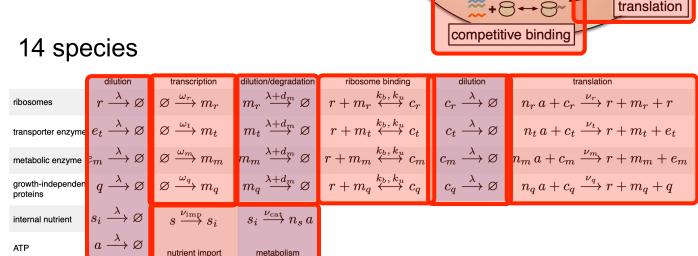
Basic mechanistic assumptions explain growth laws.

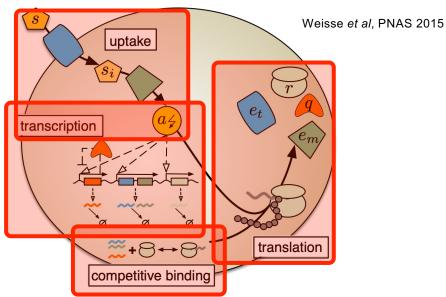


What can a more complex model teach us?

We focus on key mechanisms:

- nutrient uptake
- gene expression
- dilution

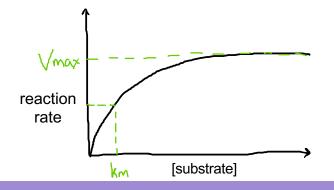


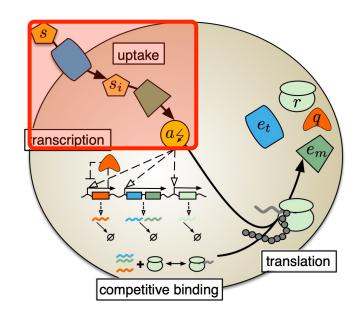




Enzymes catalyze nutrient uptake and metabolism.

Nutrient import & catabolism modelled as saturable enzymatic reactions:





Translation is an ATP-consuming process.

Repeated binding and elongation with subsequent release occur with net rate:

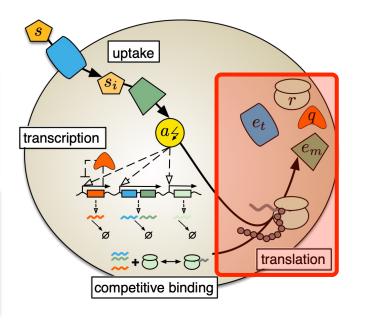
$$\nu_x = C_x \cdot \left(n_x \cdot \left(\frac{1}{K_p a} + \frac{1}{k_2} \right) + \frac{1}{k_p} \right)^{-1}$$

Assuming that release is fast, we can write this as:

$$\stackrel{k_p \gg 1}{\Rightarrow} \nu_x = \frac{C_x}{n_x}$$

$$K_p := \frac{k_1 k_2}{k_1 + k_2}, \quad \gamma_{\max} := k_2$$

 $k_p \gg 1 \
u_x = rac{C_x}{n_x} \
otag | rac{\gamma_{\max} \cdot a}{K_p + a}$ $K_p := rac{k_1 k_2}{k_{-1} + k_2}, \quad \gamma_{\max} := k_2$ elongation rate



ATP consumption by translation ~2/3 of total consumption (Russel & Cook, 1995). We assume a simplified mechanism where ATP directly binds the elongating complex:

$$R_0M \underset{k_{-1}}{\rightleftharpoons} R_0MA \xrightarrow{k_2} R_1M \underset{k_{-1}}{\rightleftharpoons} \cdots \xrightarrow{k_2} R_{n_x}M \xrightarrow{k_p} R_0 + M + P$$

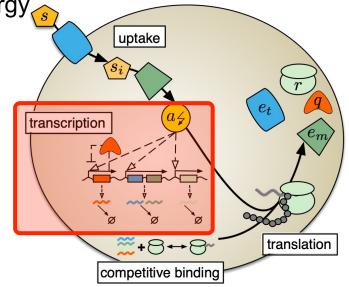


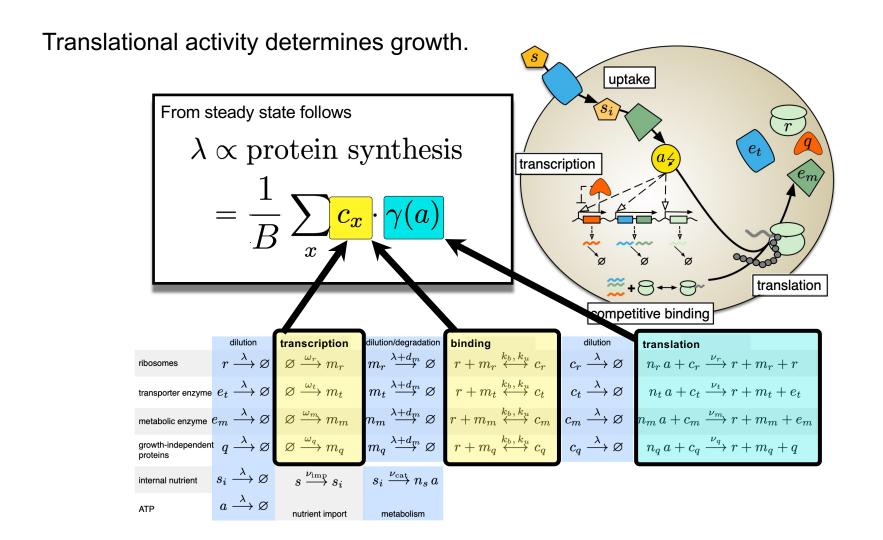
Transcription has a low contribution to energy

consumption.

We model transcription as an energy-dependent process but ignore its ATP-consumption:

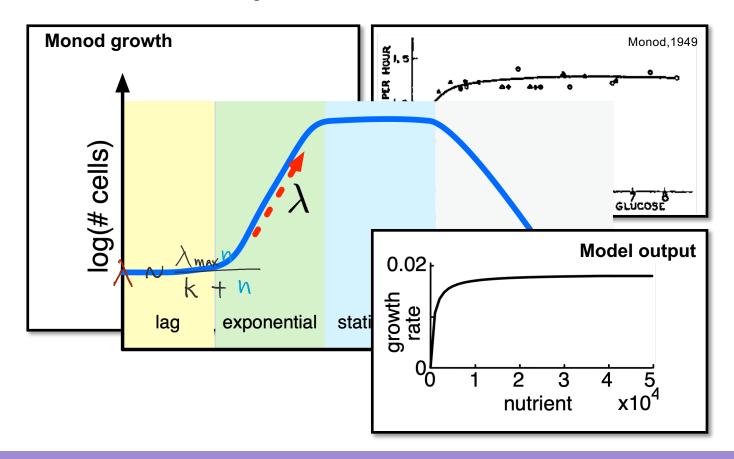
$$u_{m,x} = rac{c_x}{3n_x} \cdot rac{
ho_{\max} a}{ heta_x + a}$$
 $x \in \{e, lpha, r, p\}$



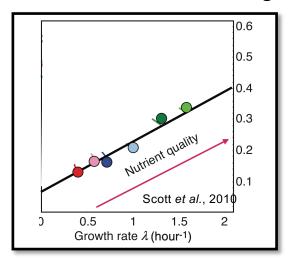


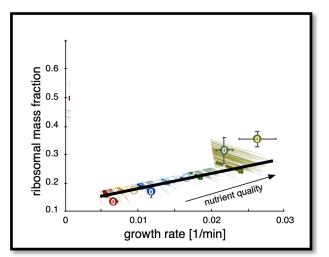


The model recovers Monod's growth law.



The model recovers the ribosomal growth laws.





Translational inhibition assuming chloramphenicol binds the mRNA-ribosome complexes, which then can't be translated anymore:

$$\begin{array}{ccc} & + & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ &$$

$$s_i \overset{
u_{\mathrm{cat}}}{\rightarrow} n_s a$$
 nutrient quality = energy yield

We can derive the empirical growth relations analytically.

1. When varying nutrient conditions mass fractions total & free ribosomes

$$\lambda = \frac{1}{\tau_{\gamma}} (\phi_R - \phi_r)$$

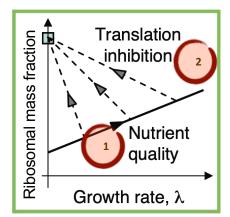
time to translate one ribosome

2. When inhibiting translation housekeeping load total ribosomes

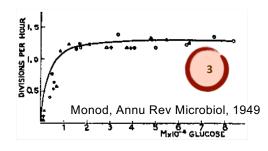
$$\lambda \simeq rac{1}{ au_e} \left(1 - \phi_q - \phi_R
ight) \cdot rac{s}{K_t + s}$$
 enzyme time constant environment

3. When changing amounts of external nutrient

$$\lambda \simeq \frac{(1 - \phi_q)s}{K_t \tau_e + (\tau_e + \tau_\gamma)s}$$

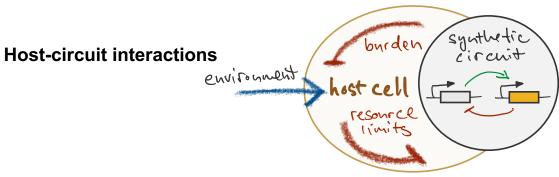


Scott & Hwa, Curr Opin Biotechnol, 2011



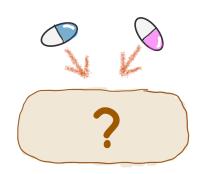


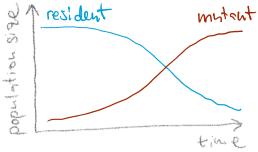
Other things we can investigate with such mechanistic model:



Evolutionary stability of cell mechanisms

Antibiotic responses



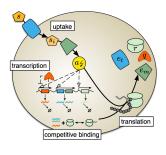


In summary

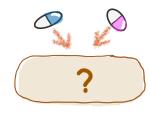
Cellular self-replication is inherently coupled with growth

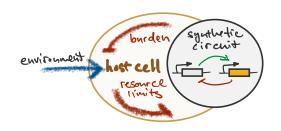
Small mechanistic models give insights on principles underpinning growth





Complexity comes at cost but can give versatility



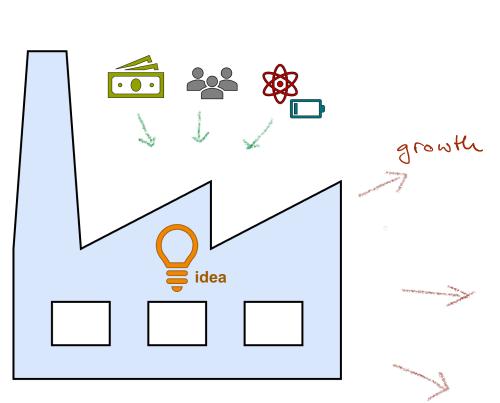


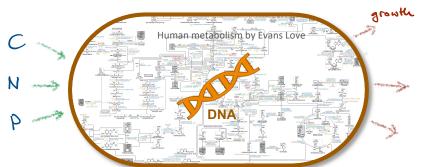
Further reading:

EPCP book chapter "Principles of growth" Weiße et al, PNAS 2015



Economic principles?





Join us!













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